

Statistics Education Research Journal

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1.1. STATISTICS EDUCATION RESEARCH JOURNAL

The *Statistics Education Research Journal (SERJ)* is a peer-reviewed electronic journal of the International Association for Statistical Education (IASE) and the International Statistical Institute (ISI). *SERJ* is published twice a year and is free.

SERJ aims to advance research-based knowledge that can help to improve the teaching, learning, and understanding of statistics or probability at all educational levels and in both formal (classroom-based) and informal (out-of-classroom) contexts. Such research may examine, for example, cognitive, motivational, attitudinal, curricular, teaching-related, technology-related, organizational, or societal factors and processes that are related to the development and understanding of stochastic knowledge. In addition, research may focus on how people use or apply statistical and probabilistic information and ideas, broadly viewed.

The *Journal* encourages the submission of quality papers related to the above goals, such as reports of original research (both quantitative and qualitative), integrative and critical reviews of research literature, analyses of research-based theoretical and methodological models, and other types of papers described in full in the Guidelines for Authors. All papers are reviewed internally by an Associate Editor or Editor, and are blind-reviewed by at least two external referees. Contributions in English are recommended. Contributions in French and Spanish will also be considered. A submitted paper must not have been published before or be under consideration for publication elsewhere.

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EDITORIAL

This last August I was fortunate enough to be able to attend several meetings, including SRTL-5 (the fifth forum on Statistical Reasoning, Thinking, and Literacy, at the University of Warwick, UK), the IASE Satellite meeting on Assessing Student Learning in Statistics (Guimarães, Portugal), and ISI-56, the biannual meeting of the International Statistical Institute (Lisbon, Portugal). Information about all of them appears in the "Past IASE Conferences" section at the end of this issue.

It was exciting to chat informally and hear presentations regarding a very wide range of studies, projects, and professional activities related to statistics education. Clearly, the international community interested in research on the learning, teaching, and understanding of statistics and probability, is growing and diversifying. From the many topics I came across, I would like to briefly highlight one that deserves special mentioning in the context of a research journal such as *SERJ*, related to the types of research data and types of evidence we encounter, and their implications for research publishing and for teaching/learning.

We often speak of "quantitative research" versus "qualitative research." Although it is recognized that both types are needed in research of an educational nature, sometimes we see researchers leaning towards one or the other. There is a somewhat tenuous relationship between quantitative and qualitative research in an area whose subject matter, statistics, is based on quantitative information, and where some of the researchers and teachers (as well as manuscript referees...) are mainly trained in quantitative methods.

However, I have now come across a number of situations where neither of these two traditional labels is sufficient, and perhaps we should refer to a third (hybrid?) kind, "Dynamic data." The need to rethink the traditional division of research into quantitative and qualitative became obvious to me this summer when listening to reports about classroom activities and studies where learners and teachers used dynamic software such as Fathom, Tinkerplots, or interactive applets such as probability simulators. In such and related cases, the data being collected by researchers (i.e., information about what students did, what they looked at, and how they thought during an activity or interpreted the results) was more complex than ever before, and sometimes quite slippery. The data accumulated over time and involved a dynamically changing mix of elements such as utterances and conversations among students or among students and teacher, different types of graphical displays, multiple "what if" trials with different aggregations or data views that the students looked at in the course of their work, results of trying different kinds of simulations, and more.

Of course, the need to collect, describe and integrate data from multiple sources, both quantitative and qualitative, has existed before the emergence of dynamic software. However, listening to reports from different studies, it became apparent that researchers are challenged by the need to capture and describe the additional fast-changing and multi-faceted data generated when dynamic software is an inherent part of the teaching/learning environment and when students are given enough time to use it in an exploratory manner. The nature of what students look at, work with, refer to, or think about is becoming more complex and harder to document, as it rapidly changes over time. Of course, all these realities place additional burden and present new demands to teachers working in a "dynamic data" environment, and have implications for the forms of needed assessments.

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