FROM DATA TO DECISION-MAKING: USING SIMULATION AND RESAMPLING METHODS TO TEACH INFERENTIAL CONCEPTS

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It is the year 2014. Despite advances in technology and the availability of interactive software and teaching tools, it is still the norm to use normality-based methods, and even look-up tables, to teach statistical inference. This puts a heavy burden on our students, who must struggle through difficult theory before they’re taught how to make decisions and draw inferences from data. Even then, do they understand what a p-value is or what a confidence interval represents? Is there a better way? Interactive computer simulations and resampling methods can help bridge the gap between graphs and summary statistics and inference, providing a gentler and more natural transition. Until recently, these methods required add-ins, specialized programs or custom code. Today, these techniques are available in mainstream statistical software. In this talk, we illustrate how to use simulations, bootstrapping, and randomization tests in JMP® to introduce sampling distributions and explore core inferential concepts.

INTRODUCTION

It is well documented that simulations and resampling methods are effective tools for teaching statistical concepts (Wood 2005, Mills 2002). The GAISE report (Aliaga et al, 2012), which provides guidelines for instruction in statistical education, recommends using technology to “perform simulations to illustrate abstract concepts.” With recent advances in computing power and expanded availability of technology, the use of computer simulation is becoming more common, and increasingly more popular, in all levels of statistics education. Today, a Google search will yield hundreds of hits on the topics of simulation, bootstrapping, and randomization tests – from articles and blogs, to sites dedicated to simulation applets and programs. Yet, as George Cobb (2007) wrote in the first issue of the journal Technology Innovations in Statistical Education,

What we teach is largely the technical machinery of numerical approximations based on the normal distribution and its many subsidiary cogs. This machinery was once necessary, because the conceptually simpler alternative based on permutations was computationally beyond our reach. Before computers statisticians had no choice. These days we have no excuse. Randomization-based inference makes a direct connection between data production and the logic of inference that deserves to be at the core of every introductory course.

This begs the question, why have many educators yet to integrate simulation and randomization methods into the classroom? One potential reason is that few textbooks (or e-books) have fully integrated randomization-based methods as a pedagogical approach, relying heavily on traditional practices (Cobb, 2013). Some recent exceptions are Tintle et al (2013), Lock et al (2013), and Good (2013), which are built around using computer simulation and resampling methods to introduce statistical inference. Lack of consistent access to computers, connection to the internet, or technical savvy to understand and utilize the methods effectively might be additional obstacles. Another potential issue may be related to the sheer number of applets, add-ins and simulators available, and the disconnect between these tools for developing statistical reasoning skills and the statistical tools required for analyzing data.

ALL METHODS, ONE PROGRAM

Statistics instructors have many objectives to satisfy in a narrow timeframe. While simulation and randomization-based methods can be more effective in introducing statistical concepts than traditional methods, getting students up to speed on accessing, using and interpreting the results from add-ins, applets or other simulation programs can be time consuming. Since these

tools generally don’t have the capacity for true data analysis, additional statistical software is often needed, requiring additional time and valuable resources. Whereas statistical software can become a resume item and hiring point for students entering the workforce, few employers will recognize specialized add-ins or simulation applets as viable statistical tools.

In this paper, we introduce a statistical tool for data analysis and exploration, JMP® 11 Pro (pronounced Jump), which can also be used for simulation and randomization-based methods. JMP® is an interactive and dynamic tool for statistical analysis and discovery, which has a rich programming language for building custom applications, add-ins and simulations. One-click bootstrapping and Monte Carlo simulations are built-in features in JMP® Pro, and a number of simulations are built into the product as sample scripts or add-ins. In addition, a comprehensive suite of freely available add-ins for educational simulations and randomizations tests can be installed and accessed through a JMP menu.

SIMULATIONS

A simulation provides an imitation of reality. Simulations in the statistical context provide an understanding of the behavior of a chosen statistic under a given set of conditions, after repeated iterations. Computer simulations facilitate the learning experience, allowing the student to individually explore and develop an understanding of difficult or abstract concepts (Mills, 2002).

A number of simulations for exploring statistical concepts are available directly in JMP®. In one program, a student can, for example, simulate data to explore the central limit theorem or tosses of a fair coin, and use built in visualization and analysis tools to explore the results of the simulations. A comprehensive collection of simulations, Concept Discovery Modules, are also available as an add-in, providing options for interactively exploring sampling distributions, confidence intervals, hypothesis tests, probability distributions, regression, and t-tests and ANOVA. An example, the Confidence Intervals for Population Proportions module, is shown in Figure 1.

![Confidence Intervals for Population Proportions module](image)

Figure 1 Confidence Intervals for Population Proportions module

For ultimate flexibility, the JMP formula editor and JSL, the JMP scripting language, can be used to create custom simulations using built-in functions. In Figure 2, the Random t function was used in a data table column formula to simulate 10,000 observations from the t distribution with 10 degrees of freedom, and results were graphed using the drag-and-drop Graph Builder®.
RANDOMIZATION TESTS

Randomization tests involve simulating the distribution of sample statistics (or test statistics) one would observe under the null hypothesis and then comparing the observed statistic to this simulated distribution, providing an empirical estimate of the p-value. Lock et al (2013), who use randomization tests to introduce concepts of hypothesis testing, provide the following rationale for this approach,

We use ideas such as randomization tests and bootstrap intervals to introduce the fundamental ideas of statistical inference. These methods are surprisingly intuitive to novice students and, with proper use of computer support, are accessible at very early stages of a course. We believe that this approach helps students realize that although the formulae may take different forms for different types of data, the conceptual framework underlying most statistical methods remains the same.
In JMP® 11, randomization tests for a variety of hypothesis tests involving proportions and means are available in a new freely-available add-in. The user specifies the type of test, the number of samples, the randomization method, the data set and the variables. Results for the randomization samples, the original sample and the selected randomization sample are displayed in separate graphs in one interactive window.

CONCLUSION

Computer simulation and technology are enabling tools, allowing statistics educators to move beyond and perhaps abandon classical methods of instruction. As George Cobb (2007) wrote in the same issue of the journal *Technology Innovations in Statistical Education*,

Just as computers have freed us to analyze real data sets, with more emphasis on interpretation and less on how to crunch numbers, computers have freed us to simplify our curriculum, so that we can put more emphasis on core ideas like randomized data production and the link between randomization and inference, less emphasis on cogs in the mechanism, such as whether 30 is an adequate sample size for using the normal approximation.

REFERENCES


